Is the Potential for International Diversification Disappearing?*

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Abstract

Quantifying the evolution of security co-movements is critical for asset pricing and portfolio allocation, and so we investigate patterns and trends in correlations and tail dependence over time using weekly returns for developed markets (DMs) and emerging markets (EMs) during the period 1973-2009. We use the standard DCC and DECO correlation models, but we also develop a nonstationary DECO model as well as a novel dynamic skewed t-copula to allow for dynamic and asymmetric tail dependence. We show that it is possible to characterize co-movements for many countries simultaneously. Correlations have significantly trended upward for both DMs and EMs, but correlations between EMs are lower than between DMs. The tail dependence has also increased for both EMs and DMs, but its level is still very low for EMs as compared to DMs. Thus, while our correlation analysis suggests that the diversification potential of EMs has reduced over time, the tail dependence analysis suggests that EMs offer diversification benefits during large market moves.

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Keywords: Asset allocation, dynamic conditional correlation (DCC), dynamic equicorrelation (DECO), dynamic copula, asymmetric dependence

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1 Introduction

Understanding and quantifying the evolution of security co-movements is critical for asset pricing and portfolio allocation. The traditional case for international diversification benefits has relied largely on the existence of low cross-country correlations. Initially, the literature studied developed markets, but over the last two decades much of the focus has shifted to the diversification benefits offered by emerging markets.\(^1\) Two critical questions, with important implications for asset allocation and international diversification, are of special interest for academics and practitioners alike.

First, how have cross-country correlations changed through time? It is far from straightforward to address this ostensibly simple question without making additional assumptions. Computing rolling correlations is subject to well-known drawbacks. Multivariate GARCH models, as for example in Longin and Solnik (1995), seem to provide a solution, but the implementation of these models using large numbers of countries is subject to well known dimensionality problems, as discussed by Solnik and Roulet (2000). As a result, most of the available evidence on the time-variation in cross-country correlations is based on factor models.\(^2\) In a recent paper, Bekaert, Hodrick, and Zhang (2009) convincingly argue that the evidence from this literature is mixed at best and state that (see p. 2591): “It is fair to say that there is no definitive evidence that cross-country correlations are significantly and permanently higher now than they were, say, 10 years ago.” Bekaert, Hodrick, and Zhang (2009) proceed to investigate international stock return co-movements for 23 DMs during 1980-2005, and find an upward trend in return correlations only among the subsample of European stock markets, but not for North American and East Asian markets.

The second question is whether correlation is a satisfactory measure of dependence in international markets, or if we need to consider different measures, notably those that focus on the dependence between tail events? This question is related to the analysis of changes in correlation as a function of business cycle conditions or stock market performance. Following the seminal paper by Longin and Solnik (2001) and the corroborating evidence of Ang and Bekaert (2002), the

\(^1\)For early studies documenting the benefits of international diversification, see Solnik (1974) for developed markets and Errunza (1977) for emerging markets. For more recent evidence, see for example Erb, Harvey and Viskanta (1994), DeSantis and Gerard (1997), Errunza, Hogan and Hung (1999), and Bekaert and Harvey (2000).

hypothesis that cross-market correlations rise in periods of high volatility has been supplanted by the notion that correlations increase in bear markets, but not in bull markets. Longin and Solnik (2001) use extreme value theory in bivariate monthly models for the U.S. with either the U.K., France, Germany, or Japan during 1959-1996. Ang and Bekaert (2002) develop a regime switching dynamic asset allocation model, and estimate it for the U.S., U.K., and German system over the period 1970-1997. Both papers estimate return exceedances at predetermined threshold values, i.e. they define the tail observations ex ante, and then compute unconditional correlations for the tail for a small sample of developed markets.

This paper substantially contributes to our understanding of both these important questions. Regarding the patterns and trends in correlations over time, we argue that recent advances make it feasible to overcome dimensionality and convergence problems in international finance applications. We characterize time-varying correlations using weekly returns during the 1973-2009 period for a large number of countries (either thirteen or seventeen EMs, sixteen DMs, as well as combinations of the EM and DM samples), without relying on a factor model. We implement models that overcome the dimensionality problems, and that are easy to estimate. To do so, we rely on the variance targeting idea in Engle and Mezrich (1996) and the numerically efficient composite likelihood procedure proposed by Engle, Shephard and Sheppard (2008). To our knowledge, we are the first to apply the composite likelihood estimation procedure, and therefore the first to be able to estimate dynamic correlation models, on large sets of international equity data using weekly returns. We use the flexible dynamic conditional correlation (DCC) model of Engle (2002) and Tse and Tsui (2002), as well as the dynamic equicorrelation (DECO) model of Engle and Kelly (2009) that can be estimated on large sets of assets using conventional maximum likelihood estimation. We thus demonstrate that it is possible to estimate correlation patterns in international markets using large numbers of countries and extensive time series, without relying on a factor model that may bias inference. Our implementation is relatively straightforward and computationally fast, which allows us to report results using several estimation approaches, while assessing the robustness of our findings.

Regarding the second question, the DECO and DCC correlation models with normal innovations do not generate the kind of tail dependence required by the data. Hence, we introduce copula approaches to capture nonlinear dependence across markets. We fit the tails of the marginal distributions using the Generalized Pareto distribution (GP), and the joint distribution is modeled using

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3 On tail dependence, see also Poon, Rockinger, and Tawn (2004). On the related topic of contagion, see for example Forbes and Rigobon (2002), Bekaert, Harvey, and Ng (2005), and Bae, Karolyi, and Stulz (2003).

time-varying copulas. We develop a novel skewed dynamic t-copula which allows for asymmetric and dynamic tail dependence in large portfolios.

Thus, we contribute to the literature in several ways. First, we demonstrate that it is possible to model correlation dynamics and tail dependence in international markets using large samples, without relying on factor models. Second, we extend existing results to a more recent period characterized by significant liberalizations for the EM sample, as well as substantial market turmoil during 2007-2009, which helps identify tail dependence. Third, we build a new correlation model with a nonstationary low-frequency component. Fourth, we develop a new fully-specified dynamic model that can capture nonlinear and asymmetric dependence in a large number of equity markets.

Our results based on DCC and DECO models are extremely robust and suggest that correlations have been significantly trending upward for both DMs and EMs. However, the correlation between DMs has been higher than the correlation between EMs at all times in the sample. For developed markets, the average correlation with other developed markets is higher than the average correlation with emerging markets. For emerging markets, the correlation with developed markets is generally somewhat higher than the correlation with the other emerging markets. However, the differences are small. When dividing our sample into four regions: EU and non-EU, Latin America and Emerging Eurasia we find that the correlation between all four regions have gone up and so has the average correlation within each region. While the range of correlations for DMs has narrowed around the increasing trend in correlation levels, this is not the case for EMs. Emerging markets thus still offer substantial correlation-based diversification benefits to investors.

Our robust finding of an upward trend in correlations is all the more remarkable because the parametric models we use enforce mean-reversion in volatilities and correlation, and we estimate the models using long samples of weekly returns. The data clearly pull the models away from the average correlation, and any reversion to the mean is temporary in the samples we investigate. In order to explicitly address the issue of nonstationarity in correlations we develop a new two-component correlation model which includes a nonstationary long-run correlation component. We refer to this model as Spline DECO and when estimated it confirms the upward trends in correlation across DMs and EMs.

We find overwhelming evidence that the assumption of multivariate normality is inappropriate. Results from the dynamic t-copula indicate substantial tail dependence. Moreover, tail dependence as measured by the skewed t-copula is asymmetric and increasing through time for both EMs and DMs. However, the most striking finding is that the level of the tail dependence is still very low at the end of the sample period for EMs as compared to DMs. Our findings on tail dependence thus suggest that EMs have offered diversification benefits for large market moves. The underlying intuition for this finding is that while financial crises in EMs are frequent, many of them are
country-specific. From this perspective the diversification benefits from adding emerging markets to a portfolio thus appear to be significant. Thus, we are able to compare the stylized facts for EMs vis-à-vis those for DMs and provide evidence corroborating the findings of Ang and Bekaert (2002) regarding the benefits of international diversification. Indeed, our results suggest that although such benefits might have lessened in the case of DMs, the case for EMs remains strong.

The paper proceeds as follows. Section 2 provides a brief outline of DCC and DECO correlation models, with special emphasis on the estimation of large systems. Section 3 presents the data, as well as empirical results on time variation in linear correlations. Section 4 builds and estimates a new set of copula models with dynamic tail dependence, asymmetry and dynamic copula correlations. Section 5 analyzes the EM correlations further and develops the new two-component correlation model that includes a nonstationary long-run correlation component. Section 6 concludes.

2 Dynamic Dependence Models for Many Equity Markets

This section outlines the various models we use to capture the dynamic dependence across equity markets. We describe how the dynamic conditional correlation model of Engle (2002) and Tse and Tsui (2002) can be implemented simultaneously on many assets.

2.1 The Dynamic Conditional Correlation Approach

In the existing literature, the scalar BEKK model has been the standard econometric approach for capturing dynamic dependence.\(^5\) The implementation of multivariate GARCH models have traditionally used a limited number of countries because of dimensionality problems.\(^6\) Further, the defining characteristic of the scalar BEKK model is that the parameters are identical across all conditional variances and covariances dynamics. This common persistence across all variances and covariances is clearly restrictive. Cappiello, Engle and Sheppard (2006), have found that the persistence in correlation differs from that in variance when looking at international stock and bond markets.\(^7\)

Equally important is the restriction that the functional form of the variance dynamic is required

\(^5\)The BEKK model is most often used to estimate factor models with a GARCH structure. See for instance DeSantis and Gerard (1997, 1998), and Carrié, Errunza, and Hogan (2007) for examples. See Ramchand and Susmel (1998), Baele (2005), and Baele and Inghilebrecht (2009) for more general multivariate GARCH models with regime switching.


\(^7\)See Kroner and Ng (1998) and Solnik and Roulet (2000) for a more elaborate discussion of the restrictions imposed in the first generation of multivariate GARCH models.
to be identical to the form of the covariance dynamic. This rules out for example the so-called leverage effect in volatility, which has been found to be an important stylized fact in equity index returns (see for example Black, 1976, and Engle and Ng, 1993). The leverage effect is really an asymmetric volatility response that captures the fact that a large negative shock to an equity market increases the equity market volatility by much more than a positive shock of the same magnitude.

Hence, we implement the flexible dynamic conditional correlation (DCC) model of Engle (2002) and Tse and Tsui (2002).\(^8\) Allowing for the leverage effect in conditional variance, we assume that the return on asset \(i\) at time \(t\) follows the dynamic

\[
\begin{align*}
  R_{i,t} &= \mu_{i,t} + \varepsilon_{i,t} = \mu_{i,t} + \sigma_{i,t} z_{i,t} \\
  \sigma^2_{i,t} &= \omega_i + \alpha_i (\varepsilon_{i,t-1} - \theta_i \sigma_{i,t-1})^2 + \beta_i \sigma^2_{i,t-1}.
\end{align*}
\]  

(2.1)  

(2.2)

Because the covariance is just the product of correlations and standard deviations, we can write

\[
\Sigma_t = D_t \Gamma_t D_t
\]

(2.3)

where \(D_t\) has the standard deviations \(\sigma_{i,t}\) on the diagonal and zeros elsewhere, and where \(\Gamma_t\) has ones on the diagonal and conditional correlations off the diagonal.

We implement the modified DCC model discussed in Aielli (2009), in which the correlation dynamics are driven by the cross-products of the return shocks

\[
\tilde{\Gamma}_t = \Omega_t + \beta_t \tilde{\Gamma}_{t-1} + \alpha_t \tilde{z}_{t-1} \tilde{z}_{t-1}^T
\]

(2.4)

where \(\tilde{z}_{i,t} = \sqrt{\tilde{\Gamma}_{ii,t}} z_{i,t}\). These cross-products are used to define the conditional correlations via the normalization

\[
\Gamma_{ij,t}^{DCC} = \tilde{\Gamma}_{ij,t} / \sqrt{\tilde{\Gamma}_{ii,t} \tilde{\Gamma}_{jj,t}}.
\]

(2.5)

This normalization ensures that all correlations remain in the \([-1, 1]\) interval.

If \(N\) denotes the number of equity markets under study then the DCC model has \(N(N-1)/2 + 2\) parameters to be estimated. Below we will study up to 17 emerging markets and 16 mature markets, thus \(N = 33\) and so the DCC model will have 530 parameters. It is well recognized in the literature that it is impossible to estimate these parameters reliably due to the need to use numerical optimization techniques, see for instance Solnik and Roulet (2000) for a discussion. In order to operationalize estimation, we follow for example DeSantis and Gerard (1997) who rely on

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\(^8\)Our findings still hold when using the BEKK approach. Results using the BEKK model are available upon request.
Taking expectations on both sides of (2.4) and solving for the unconditional correlation matrix \( \bar{\Gamma} \) of the vector \( \bar{z}_t \), yields
\[
\bar{\Gamma} = \Omega_\Gamma / (1 - \alpha - \beta). 
\]
(2.6)

Note that this relationship enables us to rewrite the DCC model in a more intuitive form
\[
\bar{\Gamma}_t = (1 - \alpha_\Gamma - \beta_\Gamma) \bar{\Gamma} + \beta_\Gamma \bar{\Gamma}_{t-1} + \alpha_\Gamma \bar{z}_{t-1} \bar{z}_{t-1}^T
\]
(2.7)

which shows that the conditional correlation in DCC is a weighted average of the long-run correlation, yesterday’s conditional correlation, and yesterday’s innovation cross-product.

Now, if we use the sample correlation matrix, \( \hat{\Gamma} = \frac{1}{T} \sum_{t=1}^{T} \bar{z}_t \bar{z}_t^T \) as an estimate of the unconditional correlation matrix, \( \bar{\Gamma} \), then the numerical optimizer only has to search in two dimensions, namely over \( \alpha_\Gamma \) and \( \beta_\Gamma \), rather than in the original 530 dimensions. Note that this implementation also ensures that the estimated DCC model yields a positive definite correlation matrix, because \( \bar{z}_t \bar{z}_t^T \) and thus \( \hat{\Gamma} \) is positive definite by construction. Appendix A contains more detail on the implementation of correlation targeting in the DCC model.

Even when using correlation targeting, estimation is cumbersome in large-dimensional problems due to the need to invert the \( N \) by \( N \) correlation matrix, \( \Gamma_t \), on every day in the sample for every likelihood evaluation. The likelihood in turn must be evaluated many times in the numerical optimization routine. More importantly, Engle, Shephard and Sheppard (2008) find that in large-scale estimation problems, the parameters \( \alpha \) and \( \beta \) which drive the correlation dynamics are estimated with bias when using conventional estimation techniques. They propose an ingenious solution based on the composite likelihood defined as
\[
CL(\alpha, \beta) = \sum_{t=1}^{T} \sum_{i=1}^{N} \sum_{j>i} \ln f(\alpha, \beta; z_{it}, z_{jt})
\]
(2.8)

where \( f(\alpha, \beta; z_{it}, z_{jt}) \) denotes the bivariate normal distribution of asset pair \( i \) and \( j \) and where correlation targeting is imposed.

The composite log-likelihood is thus based on summing the log-likelihoods of pairs of assets. Each pair yields a valid (but inefficient) likelihood for \( \alpha \) and \( \beta \), but summing over all pairs produces an estimator which is relatively efficient, numerically fast, and free of bias even in large-scale problems. We use the composite log-likelihood in all our estimations below. We have found it to be very reliable and robust, effectively turning a numerically impossible task into a manageable one. To the best of our knowledge, we are the first to apply the composite likelihood estimation procedure to
the estimation of large systems of international equity data using long time series of weekly returns, which are needed for the identification of variance and covariance patterns, and therefore the first to be able to estimate dynamic correlation models for such large systems.

### 2.2 The Dynamic EquiCorrelation Approach

The dynamic equicorrelation (DECO) model in Engle and Kelly (2009) can be viewed as a special case of the DCC model in which the correlations are equal across all pairs of countries but where this common so-called equicorrelation is changing over time. The resulting dynamic correlation can be thought of as an average dynamic correlation between the countries included in the analysis. Following Engle and Kelly (2009), we parameterize the dynamic equicorrelation matrix as

\[
\Gamma_t^{DECO} = (1 - \rho_t)I_N + \rho_t J_{N \times N}
\]

where \( \rho_t \) is a scalar, \( I_N \) denotes the n-dimensional identity matrix and \( J_{N \times N} \) is an \( N \times N \) matrix of ones.

The scalar dynamic equicorrelation, \( \rho_t \), is obtained by taking the cross-sectional average each period of the DCC conditional correlation matrix in (2.5)

\[
\rho_t = \frac{1}{N(N-1)} \left( J_{1 \times N} \Gamma_t^{DCC} J_{N \times 1} - N \right).
\]  

(2.9)

Note that subtracting \( N \) eliminates the trivial term arising from the ones on the diagonal of \( \Gamma_t^{DCC} \).

The determinant of the DECO correlation matrix is simply

\[
|\Gamma_t^{DECO}| = (1 - \rho_t)^{N-1} (1 + (N - 1) \rho_t)
\]

and from this we can derive the inverse correlation matrix as

\[
(\Gamma_t^{DECO})^{-1} = \frac{1}{(1 - \rho_t)} \left[ I_N - \frac{\rho_t}{1 + (N - 1) \rho_t} J_{N \times N} \right].
\]

The simple structure of the inverse correlation matrix ensures that the model can be estimated on large sets of assets using conventional maximum likelihood estimation. The dynamic correlation parameters, \( \alpha_\Gamma \) and \( \beta_\Gamma \) embedded in \( \rho_t \) will not be estimated with bias even when \( N \) is large.
2.3 Measuring Conditional Diversification Benefits

If correlations are changing over time, then the benefits of portfolio diversification will be changing as well. We therefore need to develop a dynamic measure of diversification benefits. First define portfolio volatility generically as

$$\sigma_{PF,t} \equiv \sqrt{w^\top \Sigma_t w}$$

Consider then the extreme case where there does not exist any diversification benefits, that is, the correlation matrix $\Gamma_t$ is a matrix of ones. The portfolio volatility in this case at time $t$ can be expressed as

$$\bar{\sigma}_{PF,t} = \sqrt{w^\top D_t J_{N \times N} D_t w} = w^\top \sigma_t$$

where $D_t$ is defined as in (2.3) and where $\sigma_t$ and $\Sigma_t$ denote respectively the vector of individual volatilities and the covariance matrix at time $t$.

The opposite extreme would correspond to each pair of assets having a correlation of $-1$ in which case it is possible to find a portfolio weight such that the portfolio volatility is $0$.

Using these upper and lower bounds of portfolio volatility, we define the conditional diversification benefit as

$$CDB_t = \frac{\bar{\sigma}_{PF,t} - \sigma_{PF,t}}{\bar{\sigma}_{PF,t}} = 1 - \frac{\sqrt{w^\top \Sigma_t w}}{w^\top \sigma_t}. \quad (2.10)$$

This measure describes the level of diversification benefits in a concise manner. It is increasing as the correlations decrease, and it is normalized to lie between $0$ and $1$.

When computing $CDB_t$ one must first decide on the portfolio weights in the vector $w$. First, each week we could choose the weights that maximize $CDB_t$.\(^9\) Second, we could construct the minimum variance portfolio each week and compute the $CDB_t$ value corresponding to this portfolio. We follow the second approach and further impose that the weights sum to one and are non-negative.

The portfolio weights and thus the $CDB_t$ will depend on the asset volatilities as well as correlations. If we want to focus on the contribution to $CDB_t$ coming from the dynamic correlations then we could assume that the conditional volatility is the same across assets but not constant across time

$$\sigma_{i,t} = \sigma_{j,t} \quad \text{for all } i, j$$

then we have

$$CDB_t^{EQV} = 1 - \frac{\sqrt{w^\top \Gamma_t w}}{w^\top J_{N \times 1}} = 1 - \sqrt{w^\top \Gamma_t w}. \quad (2.11)$$

Note that in the special case that all correlations are equal to one, the optimal weight maximizing

the measure will be $1/N$ for all assets, and $CDB_i^{EQV}$ will be zero as in the case of (2.10). If all the correlations are zero, then $CDB_i^{EQV} = 1 - \sqrt{w^Tw}$ and the optimal weights are again $1/N$. The measure is then equal to $1 - 1/N$, and therefore close to one when $N$ is large.

3 Empirical Correlation Analysis

This section contains our empirical correlation results. We first describe the different data sets that we use and briefly discuss the univariate models. We then analyze the time-variation in linear correlations. Subsequently we measure the dispersion in correlations across pairs of assets at each point in time and check if this dispersion has changed over time.

3.1 Data and Univariate Models

We employ the following three data sets:

First, from DataStream we collect weekly closing U.S. dollar returns for the following 16 developed markets: Australia, Austria, Belgium, Canada, Denmark, France, Germany, Hong Kong, Ireland, Italy, Japan, Netherlands, Singapore, Switzerland, U.K., and U.S. This data set contains 1,901 weekly observations from January 12, 1973 through June 12, 2009.

Second, from Standard and Poor’s we collect the IFCG weekly closing U.S. dollar returns for the following 13 emerging markets: Argentina, Brazil, Chile, Colombia, India, Jordan, Korea, Malaysia, Mexico, Philippines, Taiwan, Thailand, and Turkey. This data set contains 1,021 weekly observations from January 6, 1989 through July 25, 2008.

Third, from Standard and Poor’s we collect the weekly closing investable IFCI U.S. dollar returns for the following 17 emerging markets: Argentina, Brazil, Chile, China, Hungary, India, Indonesia, Korea, Malaysia, Mexico, Peru, Philippines, Poland, South Africa, Taiwan, Thailand, and Turkey. This data set contains 728 weekly returns from July 7, 1995 through June 12, 2009.

We use two emerging markets data sets because they have their distinct advantages. The IFCG data set spans a longer time period, and represents a broad measure of emerging market returns, but is not available after July 25, 2008. The IFCI data set tracks returns on a portfolio of emerging market securities that are legally and practically available to foreign investors. The index construction takes into account portfolio flow restrictions, liquidity, size and float. It continues to be updated but the sample period is shorter, which is a disadvantage in model estimation and of course in assessing long-term trends in correlation.

Table 1 contains descriptive statistics on the 1989-2008 data set. While the cross-country variations are large, Table 1 shows that the average annualized return in the developed markets was
12.06%, versus 17.68% in the emerging markets. This emerging market premium is reflective of an annual standard deviation of 33.63% versus only 18.41% in developed markets. Kurtosis is on average higher in emerging markets indicating more tail risk. But skewness is slightly positive in emerging markets and slightly negative in mature markets, suggesting that emerging markets are not more risky from this perspective. The first-order autocorrelations are small for most countries. The Ljung-Box (LB) test that the first 20 weekly autocorrelations are zero is not rejected in most developed markets but it is rejected in most emerging markets. We will use an autoregressive model of order two, AR(2), for each market to pick up this return dependence. The Ljung-Box test that the first 20 autocorrelations in absolute returns are zero is strongly rejected for all 29 markets. In the DECO and DCC models, we will employ a GARCH(1,1) model for each market to pick up this second-moment dependence. We use the NGARCH model of Engle and Ng (1993) found in equation 2.2 to account for asymmetries.

Table 2 reports the results from the estimation of the AR(2)-NGARCH(1,1) models on each market for the 1989-2008 data set. The results are fairly standard. The volatility updating parameter, $\alpha$, is around 0.1, and the autoregressive variance parameter, $\beta$, is around 0.8. The parameter $\theta$ governs the volatility asymmetry also known as the leverage effect. It is commonly found to be large and positive in developed markets and we find that here as well. Austria is the only outlier in this regard. Interestingly, the average leverage effect is much closer to zero in the emerging markets. The slightly negative average is driven largely by the unusual estimate of -3.38 for Jordan. The model-implied variance persistence is high for all countries, as is commonly found in the literature.

The Ljung-Box (LB) test on the model residuals show that the AR(2) models are able to pick up the weak evidence of return predictability found in Table 1. Impressively, the GARCH models are also able to pick up the strong persistence in absolute returns found in Table 1. Note also that the GARCH model has picked up much of the excess kurtosis found in Table 1. The remaining nonnormality will be addressed in the copula modeling below.

We conclude from Tables 1 and 2 that the AR(2)-NGARCH(1,1) models are successful in delivering the white-noise residuals that are required to obtain unbiased estimates of the dynamic correlations. We will therefore use the AR(2)-NGARCH(1,1) model in the DECO and DCC applications.

### 3.2 Correlation Patterns Over Time

Table 3 reports the parameter estimates and log likelihood values for the DECO and DCC correlation models. We report results for the three data sets introduced above. For each set of countries we estimate two versions of each model: one version allowing for correlation dynamics and another
where the correlation dynamics are shut down, and thus \( \alpha_T = \beta_T = 0 \). A conventional likelihood ratio test would suggest that the restricted model is rejected for all sets of countries, but unfortunately the standard chi-squared asymptotics are not available for composite likelihoods.

The correlation persistence \( (\alpha_T + \beta_T) \) is close to one in all models implying very slow mean-reversion in correlations. In the DECO model persistence is estimated to be essentially one, reflecting the upward trend in correlation which we now discuss.

We present time series of dynamic equicorrelations (DECOs) for several samples. The left panels in Figure 1 present results for twenty-nine developed and emerging markets for the sample period January 20, 1989 to July 25, 2008. As explained in Section 3.1, sixteen of these markets are developed and thirteen are emerging markets. We also present DECOs for each group of countries separately. We refer to this sample as the 1989-2008 sample.

The right panels in Figure 1 present results for thirty-three developed and emerging markets for the sample period July 21, 1995 to June 12, 2009. This sample contains the same sixteen developed markets, and seventeen emerging markets. There is considerable overlap between this sample of emerging markets and the one used in the left panels of Figure 1. Section 3.1 discusses the differences. We refer to this sample as the 1995-2009 sample.

The left-side panels in Figure 2 contains time series of DECOs for the group of sixteen developed markets between January 26, 1973 and June 12, 2009. We refer to this sample as the 1973-2009 sample. Figure 2 also shows results for the 1989-2008 and the 1995-2009 data for comparison.

These figures contain some of the main messages of our paper. The DECOs in Figures 1 and 2, which can usefully be thought of as the average of the pairwise correlations between all pairs of countries in the sample, fluctuate considerably from year to year, but have been on an upward trend since the early 1970s. Figure 2 shows that for the sixteen developed markets, the DECO increased from approximately 0.3 in the mid-1970s to between 0.7 and 0.8 in 2009. Figure 1 indicates that over the 1989-2009 period, the DECO correlations between emerging markets are lower than those between developed markets, but that they have also been trending upward, from approximately 0.1-0.2 in the early nineties to over 0.5 in 2009.

Because the DECO approach models correlation as time-varying with a model-implied long-run mean, one may wonder whether the sample selection strongly affects inference on correlation estimates at a particular point in time. Figure 2 addresses this issue by reporting DECO estimates for the sixteen developed markets for three different sample periods. Whereas there are some differences, the correlation estimate at a particular point in time is remarkably robust to the sample period used, and the conclusion that correlations have been trending upward clearly does not depend on the sample period used. Comparing the left and right panels of Figure 1, it can be seen that a similar conclusion obtains for the emerging markets, even though this comparison is more tenuous as
the sample composition and the return data used for the emerging markets are somewhat different across panels.

3.3 Cross-Sectional Differences in Dependence

The DECO correlations give us a good idea of the evolution of correlation over time in a given sample of markets. They can usefully be thought of as an average of all possible permutations of pairwise correlations in the sample. The next question is how much cross-sectional heterogeneity there is in the correlations. The DCC framework discussed in Section 2.1 is designed to address this question. It yields a time-varying correlation series for each possible permutation of markets in the sample.

Reporting on all these time-varying pairwise correlation paths is not feasible, and we have to aggregate the correlation information in some way. Figures 2-4 provide an overview of the results. The right-side panels in Figure 2 provide the average across all markets of the DCC paths, and compare them with the DECO paths. The top-right panel provides the average DCC for the sixteen developed markets from 1973 through 2009. The middle-right panel provides the average DCC for the same sixteen markets for the 1989-2008 sample period, and the bottom-right panel for the 1995-2009 period. The left-side panels provide the DECO correlations. Figure 2 demonstrates that the DECO can indeed be thought of as an average of the DCCs. Moreover, Figure 2 demonstrates that the average DCC correlation at each point in time is robust to the sample period used in estimation, as is the case for the DECO.10

Figure 3 uses the 1989-2008 sample to report, for each of the twenty-nine countries in the sample, the average of its DCC correlations with all other countries using light grey lines. Figure 3.A contains the 16 developed markets and Figure 3.B contains the 13 emerging markets. While these paths are averages, they give a good indication of the differences between individual countries, and they are also informative of the differences between developed and emerging markets. In order to further study these differences, each figure also gives the average of the market’s DCC correlations with all (other) developed markets using black lines and all (other) emerging markets using dark grey lines. Figure 3 yields some very interesting conclusions. First, the DCC correlation paths display an upward trend for all 29 countries, except Jordan. Second, for developed markets the average correlation with other developed markets is higher than the average correlation with emerging markets at virtually each point in time for virtually all markets. Third, for emerging markets the

10In Figure 3, and throughout the paper, we report equal-weighted averages of the pairwise correlations from the DCC models. Value-weighted correlations (not reported here) also display an increasing pattern during the last 10-15 years. Note that in the benchmark DECO model all pairwise correlations are identical and so the weighting is irrelevant.
correlation with developed markets is generally higher than the correlation with other emerging markets. However, the difference between the two correlation paths is much smaller than in the case of developed markets. In several cases the average correlation paths are very similar. Note that in Figure 3.A the trend patterns for European countries are also not very different from those for other DMs. Notice in particular that the correlations for Japan and the US have increased just as for the European countries during the last decade even if the level of correlation is still somewhat lower in those two cases. Inspection of the pairwise DCC paths, which are not reported because of space constraints, reveals that the trend patterns are remarkably consistent for almost all pairs of countries, and there is no meaningful difference between European countries and other DMs.

Figure 3 reports the average correlation between the DCC of each market and that of other markets. It could be argued that instead the correlation between each market and the average return of the other markets ought to be considered. We have computed these correlations as well. While the correlation with the average return is nearly always higher than the average correlation from Figure 3, the conclusion that the correlations are trending upwards is not affected. In order to save space we do not show the plots of the correlation with average returns on other markets.

We can use the correlation paths from the DCC model to assess regional patterns in correlation dynamics. Figure 3.C does exactly this. We divide our 16 DMs into two regions (EU and non-EU) and we divide our 13 EMs into another two EM regions: Latin American and Emerging Eurasia. Using the DCC model’s country-specific correlation paths we report in Figure 3.C the average correlation within and across the four regions. Strikingly, Figure 3.C shows that the increasing correlation patterns are evident within each of the four regions and also across all the six possible pairs of regions. The highest levels of correlation are found in the upper-left panel which shows the intra-EU correlations. The lowest level of correlations are found in the bottom-right panel which shows the intra Emerging Eurasia correlations.

Figure 3 does not tell the entire story, because we have to resort to reporting correlation averages due to space constraints. Figure 4 provides additional perspective by providing correlation dispersions for the developed markets, emerging markets, and all markets respectively. In particular, at each point in time, the top panel in Figure 4 considers all DCC correlations for the sixteen developed markets, and the shaded area shows the range between the 10th and 90th percentile of these pairwise correlations. The middle panel in Figure 4 reports the same statistics for the emerging markets for the 1989-2008 sample and the bottom panel shows all 29 markets together. While the increasing level of correlations is evident, the range of correlations seems to have narrowed

\[11\] The European Union (EU) includes Austria, Belgium, Denmark, France, Germany, Ireland, Italy, Netherlands, and the UK. Developed Non-EU includes Australia, Canada, Hong Kong, Japan, Singapore, Switzerland, and the US. Latin America includes Argentina, Brazil, Chile, Colombia, and Mexico. Emerging Eurasia includes India, Jordan, Korea, Malaysia, Philippines, Taiwan, Thailand, and Turkey.
for developed markets, widened a bit for emerging markets, and the range width seems to have stayed roughly constant for all markets taken together. The wide range of correlations found within emerging markets again suggests that the potential for diversification benefits are greater here.

Figure 5 plots the conditional diversification benefit measures developed in equations (2.10) and (2.11) for developed, emerging, and all markets using the dynamic correlations from the DCC model. The optimally weighted portfolio in Figure 5 shows a decreasing trend in diversification benefits in DMs: Correlations have been rising rapidly and the benefits of diversification have been decreasing during the last ten years. Diversification benefits have also somewhat decreased in emerging markets but the level of benefits is still much higher than in developed markets. When combining the developed and emerging markets, the diversification benefits are declining as well but the level is again much higher than when considering developed markets alone. Emerging markets thus still offer substantial correlation-based diversification benefits to investors.

4 Dynamic Nonlinear Diversification

We have relied on the multivariate normal distribution to implement the dynamic correlation models. The multivariate normal distribution is the standard choice in the literature because it is convenient and because quasi maximum likelihood results ensure that the dynamic correlation parameters will be estimated consistently even when the normal distribution assumption is incorrect, as long as the dynamic models are correctly specified.

While the multivariate distribution is a convenient statistical choice, the economic motivation for using it is more dubious. It is well-known (see for example Longin and Solnik, 2001) that international equity returns display extreme correlations not captured by the normal distribution: Large moves in international equity markets are highly correlated, which is of course crucial for assessing the benefits of diversification. The dynamic correlation models considered above have some ability to generate extreme correlations but likely not to the degree required by the data. In this section, we therefore go beyond the dynamic multivariate normal distributions implied by the DCC and DECO models discussed above and introduce dynamic copula models which have the potential to generate empirically relevant levels of extreme correlations.

Copulas are an extremely convenient tool that allows us to build a multivariate distribution for a set of assets from any choice of marginal distributions for each individual asset. It is crucial to first specify appropriate and potentially non-normal marginal distributions in order to ensure that the copula-based multivariate distribution will be well specified.\textsuperscript{12}

\textsuperscript{12}McNeil, Frey and Embrechts (2005) provide an authoritative review of the use of copulas in risk management.
4.1 Building the Marginal Distributions

In order to allow for flexible marginal distributions we use a kernel approach to nonparametrically estimate the empirical cumulative distribution function (EDF) of each standardized return time series, \( z_{i,t} \). Recall from (2.1) that

\[
z_{i,t} = \frac{R_{i,t} - \mu_{i,t}}{\sigma_{i,t}}
\]

where \( \mu_{i,t} \) is obtained from an AR model.

Nonparametric kernel EDF estimates are well suited for the interior of the distribution where most of the data is found, but tend to perform poorly when applied to the tails of the distribution. Fortunately, a key result in extreme value theory shows that the Generalized Pareto distribution (GP) fits the tails of a wide variety of distributions. Thus we fit the tails of the marginal distributions using the GP.

The marginal densities are constructed by combining the kernel EDF for the central 80% of the distribution mass with the GP distribution for the two tails. We write the cumulative density function as

\[
\eta_i = F_i(z_i)
\]

We refer to McNeil (1999) and McNeil and Frey (2000) for more details on our approach.

4.2 Modeling Multivariate Nonnormality

The most widely applied copula function is built from the multivariate normal distribution and referred to as the Gaussian copula. Though convenient to use, it is not flexible enough to capture the tail dependence in asset returns.\(^{13}\) We therefore build our analysis on the \( t \)-copula which is constructed from the multivariate standardized student’s \( t \) distribution. The \( t \)-copula cumulative density function is defined as

\[
C(\eta_1, \eta_2, \ldots, \eta_N; \Psi, \nu) = t_{\Psi, \nu}(t^{-1}_\nu(\eta_1), t^{-1}_\nu(\eta_2), \ldots, t^{-1}_\nu(\eta_N))
\]

where \( t_{\Psi, \nu}(\cdot) \) is the multivariate standardized student’s \( t \) density with correlation matrix \( \Psi \) and \( \nu \) degrees of freedom. \( t^{-1}_\nu(\eta_i) \) is the inverse cumulative density function of the univariate Student’s \( t \) distribution, and the marginal probabilities \( \eta_i = F_i(z_i) \) are from (4.1). More details on the \( t \)-copula are provided in Appendix B.

Note that the matrix \( \Psi \) captures the correlation of the fractiles \( z^*_i \equiv t^{-1}_\nu(\eta_i) \) and not of the return shock \( z_i \). We refer to \( \Psi \) as the copula correlation matrix in order to distinguish it from the

\(^{13}\)Estimation results from a normal copula with dynamic correlation are available upon request.
conventional matrix of linear correlation studied above. Notice also that

\[ z^*_i \equiv t^{-1}_\nu(\eta_i) = t^{-1}_\nu(F_i(z_i)) \]

so that if the marginal distributions \( F_i \) are close to the \( t_v \) distribution then \( z^*_i \) will be close to \( z_i \) and the copula correlations will be close to the conventional linear correlations.

### 4.3 Allowing for Dynamic Copula Correlations

The combination of copula functions with the dynamic correlation models considered above is straightforward. We again rely on the parsimonious DCC and DECO approaches. Using the fractiles \( z^*_i \equiv t^{-1}_\nu(\eta_i) \) instead of the return shock in the DCC model provides dynamic matrices for the conditional copula correlations as follows

\[
\bar{\Psi}_t = \Omega_\Psi + \beta_\Psi \bar{\Psi}_{t-1} + \alpha_\Psi \tilde{z}^*_t \tilde{z}^*_T
\]

where \( \tilde{z}^*_{i,t} = z^*_{i,t} \bar{\Psi}_{ii,t} \). These cross-products are used to define the conditional copula correlations via the normalization

\[
\Psi_{ij,t}^{DCC} = \bar{\Psi}_{ij,t} / \sqrt{\bar{\Psi}_{ii,t} \bar{\Psi}_{jj,t}}.
\]

In the empirics below we will refer to the model combining the copula density in (4.2) and the copula correlation dynamics in (4.3) as the DCC \( t \)-copula model. We also estimate the DECO \( t \)-copula in which the dynamic copula correlations are identical across all pairs of assets. The parameters in these dynamic \( t \)-coupla models are easily estimated using the composite likelihood approach discussed above.

### 4.4 Allowing for Multivariate Asymmetry

The presence of asymmetry in dependence in international equity portfolios has long been established, see for example Longin and Solnik (2001) and Ang and Bekaert (2002). Unfortunately, the standard \( t \)-copula model considered so far implies symmetry in the tail dependence. To address this problem, we consider the skewed \( t \) distribution discussed in Demarta and McNeil (2005) which we use to develop an asymmetric \( t \)-copula. In parallel with the symmetric \( t \)-copula we can write the skewed \( t \)-copula cumulative density function

\[
C(\eta_1, \eta_2, \ldots, \eta_N; \Psi, \lambda, \nu) = t_{\Psi,\lambda,\nu}(t^{-1}_{\lambda,\nu}(\eta_1), t^{-1}_{\lambda,\nu}(\eta_2), \ldots, t^{-1}_{\lambda,\nu}(\eta_N))
\]
where \( \lambda \) is a new asymmetry parameter, \( t_{\Psi,\lambda,v}(\cdot) \) is the multivariate asymmetric standardized student’s \( t \) density with correlation matrix \( \Psi \), and \( t^{-1}_{\lambda,v}(\eta_i) \) is the inverse cumulative density function of the univariate asymmetric Student’s \( t \) distribution. The univariate probabilities \( \eta_i = F_i(z_i) \) are from (4.1) as before. The asymmetric \( t \)-copula is built from the asymmetric multivariate \( t \) distribution and the symmetric \( t \)-copula is nested when \( \lambda = 0 \). Appendix C provides the details needed to implement the asymmetric \( t \)-copula. Notice that the semiparametric approach to the marginal distributions capture any univariate skewness present in the equity returns. The new \( \lambda \) parameter captures multivariate asymmetry.

For the sake of parsimony in our high-dimensional applications we report on a version of the skewed \( t \)-copula where the asymmetry parameter \( \lambda \) is a scalar. It is straightforward to develop a more general version of the skewed \( t \)-copula allowing for an \( N \)-dimensional vector of \( \lambda \)s. But such a model is not easily estimated on a large number of countries.

Asymmetry in the bivariate distribution of asset returns has generally been modeled using copulas from the Archimedean family which include the Clayton, the Gumbel, and the Joe-Clayton specifications.\(^{14}\) These models are rarely used in high-dimensional applications. The skewed \( t \) copula is parsimonious, tractable in high dimension, and flexible allowing us to model non-linear and asymmetric dependence with the degree of freedom parameter, \( \nu \), and the asymmetry parameter, \( \lambda \), while retaining a dynamic conditional correlation matrix, \( \Psi \).

### 4.5 Allowing for Dynamic Degrees of Freedom

So far we have assumed that the degree of freedom parameter, \( \nu \) is constant over time. Allowing for dynamics in \( \nu \) and thus in the degree of nonnormality can be done in several ways. Inspired by Engle and Rangel (2008, 2010) we assume that the degree of freedom evolves as a quadratic trend

\[
\nu_t = e^{\nu} \exp \left( w_0^\nu t + w_1^\nu (t - t_0)^2 \right),
\]

where we impose a lower bound on the dynamic so that the degree of freedom \( \nu_t \) is above the number required for finite second moments which is two in the symmetric case and four in the asymmetric case.\(^{15}\)

\(^{14}\)See for example Patton (2004, 2006).
\(^{15}\)Engle and Rangel (2008, 2010) model multiple quadratic splines thus allowing for structural breaks in the quadratic part of the trend. Our results are qualitatively similar when allowing for multiple splines functions.
4.6 Defining Tail Dependence

The various $t$-copula models developed above generalize the normal copula by allowing for non-zero dependence in the tails. One way to measure the lower tail dependence is via the probability limit

$$
\tau^L_{i,j} = \lim_{\zeta \to 0} \Pr[\eta_i \leq \zeta | \eta_j \leq \zeta] = \lim_{\zeta \to 0} \frac{C(\zeta, \zeta)}{\zeta}
$$

where $\zeta$ is the tail probability. The upper tail dependence can similarly be defined by

$$
\tau^U_{i,j} = \lim_{\zeta \to 1} \Pr[\eta_i \geq \zeta | \eta_j \geq \zeta] = \lim_{\zeta \to 1} \frac{1 - 2\zeta + C(\zeta, \zeta)}{1 - \zeta}
$$

The normal copula has the empirically dubious property that this tail dependence is zero whereas it is positive in the various $t$-copula models we develop.\(^{16}\)

In the conventional symmetric $t$-copula models the lower and upper tail dependences are identical, that is $\tau^L_{i,j} = \tau^U_{i,j}$. Based on the work by Longin and Solnik (2001) and Ang and Bekaert (2002) we suspect that this symmetry is not valid in international equity index returns and we therefore investigate the upper and lower tail dependence separately using the skewed $t$ copula model developed above.

4.7 Empirical Tail Dependence

The empirical results in Section 3 demonstrate that it is feasible to characterize dynamic correlations between a large number of markets. While these results are of great interest, it is worthwhile keeping in mind that correlation is inherently a flawed concept to analyze financial markets, because it relies on normality, and the deviations of normality for (international) stock returns are well documented. The methods developed in this section show that it is feasible to analyze dependence more generally in international stock returns using a fully-specified conditional distribution model for a large number of markets.

When characterizing multivariate dependence using the DCC and DECO models, the normality assumption enters in two critical ways: First, the marginal distribution of returns for each country is assumed to be normal; Second, the joint distribution is also assumed to be normal. The $t$ copula introduced in Section 4.2 and the skewed $t$-copula introduced in Section 4.4 allow us to address the appropriateness of these assumptions.

Table 4 reports the parameter estimates and likelihood values of the different $t$ copula models we consider. The top row shows the DCC copulas, the second row the DECO copulas, and the third row

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\(^{16}\)See Patton (2006) for an application of the extreme dependence measure to exchange rates.
the DECO copulas with dynamic degree of freedom. The left column shows the symmetric \(t\) copulas
and the right column shows the skewed \(t\)-copulas. Note that the copula correlation persistence is—as was the case in Table 3—very close to 1 in all models.

Comparing the symmetric to the asymmetric version of the \(t\)-copula, we observe that the introduction of the asymmetry parameter does not seem to impact much the correlation parameters nor the degree of freedom. This suggests that the asymmetry parameter captures a different dimension of dependence. In the DCC copulas the asymmetry parameter provides a modest increase in the likelihood but in the more restricted DECO case the asymmetry model increases the likelihood much more. Comparing the DECO copulas with constant degree of freedom to those with dynamic degree of freedom we see that the increase in likelihood is modest when allowing for spline dynamics in \(v_t\).

Figure 6 plots the dynamic measure of tail-dependence for the skewed \(t\)-copula for the DCC (left panels) and the DECO (right panels) models. We report the average of the bivariate tail dependence across all pairs of countries.\(^{17}\) In each graph, the dark line depicts the evolution of the upper tail dependence, while the gray line is for the lower tail dependence.\(^{18}\) The tail dependence measure depends on the degree of freedom, \(v\), the copula correlation, \(\Psi_{i,j}\), and the asymmetry parameter, \(\lambda\). Figure 6 shows quite dramatic differences across markets. The tail dependence in developed markets has risen markedly during the last twenty years. Remarkably, the emerging market tail dependence measures in the middle panel of Figure 6 are much lower than the developed market measures and they are only mildly trending upwards over time. The all markets case in the bottom row of Figure 6 indicates that while the tail dependence is rising, it is still much lower than for the developed markets alone. From this perspective, the diversification benefits from adding emerging markets to a portfolio appear to be large compared to those offered by developed markets, even if these benefits are getting smaller over time. In all cases, the tail dependence is higher for the lower tail than for the upper tail echoing Long and Solnik’s (2001) finding of downside threshold correlations that are much larger than their upside counterparts.

\(^{17}\)The tail dependence concept introduced above is inherently bivariate and not easily generalized to the high-dimensional case. In higher dimension, tail dependence is defined as the probability limit of all variables being below a threshold conditional on a subset of them being below the same threshold. However, in a portfolio context, it is not obvious how that conditioning subset should be defined. In order to convey the empirical evolution of tail dependence for many countries, we report the average of the bivariate tail dependence across all pairs of countries.

\(^{18}\)To the best of our knowledge a closed form solution is not available for the tail dependence measure in the skewed \(t\) copula. We therefore approximate by simulation using \(\zeta = 0.001\).
5 Exploring the Results

Several questions arise from our analysis so far.

First, our key finding above is that the benefits from diversification across developed markets have largely disappeared, but that the benefits from diversifying across emerging markets are still intact. Given the significant easing of cross-border capital flow controls and increasing levels of market integration, it would be important to investigate their effect on correlation dynamics for EMs.\textsuperscript{19} We run panel regressions that suggest a positive and significant relationship between market openness and EM correlation but not between the degree of market integration and EM correlation. These findings are consistent with prevailing theory.

Second, we employ mean-reverting models in the analysis above. These models should bias us against finding long-term trends in correlation. Nevertheless the sample-paths we extract from the models display increasing long-term trends in correlation. A natural question to ask is if these patterns are confirmed in a model that explicitly allows for non-stationarity in the correlation dynamics? We develop such a model below and show that they are.

Finally we ask if a fully model-free (but very ad-hoc) approach confirms the long-term upward trending correlation paths. It does.

5.1 EM Correlation, Volatility and Market Integration

We first investigate the impact of financial development and integration on correlation in emerging markets. To this end we first rely on Bekaert (1995) and Edison and Warnock (2003) who use a direct measure of \textit{de jure} market openness. Their measure is defined as the ratio of the market capitalizations of the investable and global indexes from S&P/IFC and we denote it by “MCR” below. The IFC Global (IFCG) index is designed to represent the market portfolio for each country, whereas the IFC Investable (IFCI) index is designed to represent a portfolio of domestic equities that are available to foreign investors. When MCR measure is one, the market capitalization of the investable index is equal to that of the market-wide index indicating that all of that countries’ stocks are available to foreign investors.

We also consider a measure of emerging market integration based on the theoretical model of Errunza and Losq (1985). The empirical measure is constructed in Carrieri, Chaieb, and Errunza (2010) and we refer to it as “EMI” below. The MCR and EMI measures have an average correlation of $-0.10$ and so clearly measure different aspects of emerging market development.

Due to MCR and EMI data availability, our sample is restricted to the period August 1995 to

\textsuperscript{19}See Bekaert et al (2008), and Carrieri et al (2010) for the evolution of market integration for EMs.
December 2006 for the 17 emerging markets in the IFCI index. As $MCR$ and $EMI$ are available on a monthly basis, we average the weekly GARCH volatilities and the DCC correlations each month. We consider different dependent variables. First, as in Figure 3a, we examine the effect of market development and integration on the average DCC correlations for each EM country. We consider three sets of correlations for each EM country: The average correlation with other EMs, the average correlation with DMs, or the average correlation with all other markets. Then, we investigate the effect of $MCR$ and $EMI$ on log EM volatility.

To investigate the impact of $MCR$ and $EMI$ on emerging market correlation we first estimate a panel regression of the form

$$
\rho^E_{i,t} = b_{i,0} + b_1 \tau + b_2 MCR_{i,t} + b_3 EMI_{i,t} + b_4 \log(\sigma^E_{i,t}) + b_5 \log(\sigma_{i,t}) + \epsilon_{i,t}, \quad i = 1, \ldots, N_{EM} \tag{5.1}
$$

where the left-hand-side variable $\rho^E_{i,t}$ is the average correlation between EM country $i$ and all other EM countries in month $t$. On the right-hand-side $b_{i,0}$ is a country specific fixed effect, $\tau$ is a time trend, and we also include $\sigma^E_{i,t}$ which denotes the average volatility across EMs in month $t$, and $\sigma_{i,t}$ which is EM country $i$’s own volatility. Following Petersen (2009), we compute White standard errors adjusted for within cluster (country) correlation. We consider specifications that include $MCR$ and $EMI$ separately as well as both together.

Panel A in Table 5 shows that the correlation time-trend is significantly positive in all three specifications confirming the visual impression of upward trending correlations in Figures 1-3. The market cap ratio $MCR$ is positive and significant whereas the market integration indicator $EMI$ is positive but not significant. This insignificance is not surprising as financial theory does not predict a relationship between correlation and market integration. The average EM volatility, $\sigma_{EM,t}$ is significantly positive which is often found in the risk management literature: correlations tend to rise when volatility rises which clearly lowers the benefits of diversification.

In Panel B of Table 5 we estimate

$$
\rho^D_{i,t} = b_{i,0} + b_1 \tau + b_2 MCR_{i,t} + b_3 EMI_{i,t} + b_4 \log(\sigma^D_{i,t}) + b_5 \log(\sigma_{i,t}) + \epsilon_{i,t}, \quad i = 1, \ldots, N_{EM} \tag{5.2}
$$

where the left-hand-side variable $\rho^D_{i,t}$ is now the average correlation between EM country $i$ and each DM country in month $t$. The variable $\sigma^D_{i,t}$ is now the average volatility across DMs. The results in Panel B shows that the time trend is again significantly positive in all three specifications. The market openness and integration variables, $MCR$ and $EMI$ are positively related to the average EM correlation with DMs but $EMI$ is not significant. Somewhat surprisingly $\sigma^D_{i,t}$ appears to be negatively related to $\rho^D_{i,t}$ although the relationship is not significant.
Panel C in Table 5 shows the results from the regression

$$\rho_{i,t}^{All} = b_{i,0} + b_{1}\tau + b_{2}MCR_{i,t} + b_{3}EMI_{i,t} + b_{4}\log (\sigma_{All,t}) + b_{5}\log (\sigma_{i,t}) + \epsilon_{i,t} \quad i = 1, ..., N_{EM} \quad (5.3)$$

where the left-hand-side variable $\rho_{i,t}^{All}$ is the average correlation between EM country $i$ and all other countries in month $t$. On the right-hand-side we now include $\sigma_{All,t}$ which denotes the average volatility across all markets in month $t$. Panel C shows that the time trend is again positive and significant and so is MCR whereas EMI is not significant but still positive. Volatility is not significant in this case.

In summary, we find that the EM correlations have clearly trended upwards in this period. They are related to market openness as measured by share of market cap available to foreign investors. However, the increase in correlation is not significantly related to the measure of financial integration implied by the Errunza and Losq (1985) model of mild market segmentation.

### 5.2 Nonstationary Correlation Dynamics

The correlation regressions in Table 5 show a very clear pattern: The simple linear time-trend in correlation is positive and strongly significant in all cases. This finding suggests that the mean-reverting DCC and DECO models considered so far may be inadequate at fully describing the evolution of international equity index correlations over time. The mean-reverting models will try to pull the correlation path back down towards the unconditional mean even if the observed returns keep pushing the correlation paths higher. Even if the correlations were not trending up one could reasonably argue that a constant long-run correlation is unrealistic for the relatively long time-series that we are analyzing here.

In this section we therefore propose a new way to model a slowly varying long-run component in correlation. Engle and Rangel (2008) model low-frequency dynamics in volatility using an extended GARCH model that features a dynamic long-run component given by a quadratic exponential spline. Engle and Rangel (2010) develop a Factor Spline GARCH for covariance by using a quadratic spline for the market stationary variance and each asset's idiosyncratic long run risks. We try to avoid imposing a factor structure and instead use the Spline GARCH idea in a DECO correlation framework. We assume that the long-run component of correlation evolves as a quadratic trend

$$\rho_t^{LR} = \Lambda \left( c + w_0 t + w_1 (t - t_0)^2 \right) \quad (5.4)$$

where the double logistic function $\Lambda(x) = \frac{1 - e^{-x}}{1 + e^{-x}}$ is used to restrict $\rho_t^{LR}$ to be between $-1$ and 1. Our results are qualitatively similar when we generalize (5.4) to allow for multiple quadratic pieces
each with separate coefficients as is done in Engle and Rangel (2008, 2010).

Our DECO correlation dynamics are built from the DCC model as before, but the constant matrix of unconditional correlations, $\bar{\Gamma}$, is replaced by

$$\bar{\Gamma}^{LR}_t = (1 - \rho_t^{LR}) I_N + \rho_t^{LR} J_{N \times N}$$

so that we now have the dynamic

$$\bar{\Gamma}_t = (1 - \alpha_t - \beta_t) \bar{\Gamma}^{LR}_t + \beta_t \bar{\Gamma}_{t-1} + \alpha_t \bar{z}_{t-1} \bar{z}_{t-1}^T. \quad (5.5)$$

We also need the normalization in (2.5) and the DECO restriction in (2.9).

The estimation results are reported in Table 6. Comparing log likelihoods with the left side of Panel B in Table 3, we see that the improvements in likelihood compared with the standard DECO model are quite modest. The simple DECO model with very high persistence seems to be able to adequately capture the correlation pattern over time. Comparing the Spline DECO likelihoods with the special case of no stochastics ($\alpha_t = \beta_t = 0$) shows that the spline function alone is capable of capturing the correlation dynamics quite well.

The right panels of Figure 7 shows the evolution of total correlation as well as the dynamic long-run correlation in the new Spline DECO model. For comparison, the basic DECO correlations from Figure 1 are repeated in the left panels of Figure 7. The dramatic upward trend in correlation is clear in both models. It is quite striking that the flexible exponential-quadratic Spline DECO model we develop implies an almost linearly rising trend in correlation through the recent decade.

### 5.3 Model-Free Correlations

The Spline DECO model developed above is of course just one approach to capturing potential non-stationarity in the correlation dynamic. However, any parametric approach will require modeling decisions that could be brought into question. We therefore end our analysis with a completely model-free (but not assumption free) alternative to correlation estimation.

Figure 8 plots the average (across all pairs of countries) model-free rolling correlations using a relatively short 6-month estimation window (denoted by grey lines) and using a relatively long 2-year estimation window (denoted by black lines). Both estimates use weekly returns to compute the rolling correlations.

Figure 8 shows that it is not the DECO model structure nor the Spline DECO model structure that are driving the upward-sloping trend result. The model-free estimates of dynamic correlation in Figure 8 show the same upward trend in correlation evident in Figures 1 and 7. The model-
free estimates of dynamic correlation have the disadvantage that they depend greatly on the width of the data window chosen: A long window will result in stable but potentially biased estimates of the true dynamic correlation whereas a very short window will result in very noisy estimates. The dynamic models we apply have the great advantage of letting the data choose—via maximum likelihood estimation—the optimal weights on past data points.

6 Summary and Conclusion

We characterize time-varying correlations using long samples of weekly returns for systems consisting of large number of countries. We implement models that overcome econometric complications arising from the dimensionality problem, and that are easier to estimate, using variance targeting and the composite likelihood procedure. Results based on the DCC and the DECO as well as on our new Spline DECO model are extremely robust and suggest that correlations have been significantly trending upward for both the DMs and EMs. Correlations between DMs have exceeded correlations between EMs throughout the 1989-2009 period. Moreover, for developed markets, the average correlation with other developed markets is higher than the average correlation with emerging markets. For emerging markets, the correlation with developed markets is generally somewhat higher than the correlation with the other emerging markets. However, the differences are small. While the range of correlation for DMs has narrowed around the increasing trend in correlation levels, this is not the case for EMs where the range instead appears to have widened.

We develop a novel skewed dynamic t-copula which allows for asymmetric and dynamic tail dependence in large portfolios. Results from the dynamic t-copula indicate substantial and asymmetric tail dependence with lower tail dependence being larger than upper tail dependence. Moreover, tail dependence as measured by the t-copula is increasing through time for both EMs and DMs. The level of the tail dependence is still very low at the end of the sample period for EMs as compared to DMs. Therefore, while the correlation analysis suggests that the diversification potential of EMs has decreased over time, our findings on tail dependence indicate significant diversification opportunities, due to the fact that while equity market crises in EMs are frequent, many of them are country-specific. From this perspective, our results suggest that although diversification benefits might have lessened in the case of DMs, the case for EMs remains strong.

These results have very important implications for portfolio management, and it may prove interesting to explore them in future work. It may also prove useful to investigate the robustness of our findings to allowing for multiple regimes, or to the inclusion of multiple stochastic components, as for example in the model of Colacito, Engle, and Ghysels (2009). Our new Spline DECO model represents an initial step in this direction.
References


Appendix

Appendix A. Correlation Targeting in DCC

Correlation targeting in the DCC model allows us to significantly reduce the number of parameters estimated via numerical optimization of the likelihood function. In total we need to estimate \( \alpha_T \), \( \beta_T \), and \( \tilde{\Gamma} \) in the DCC recursion

\[
\tilde{\Gamma}_t = (1 - \alpha_T - \beta_T) \tilde{\Gamma} + \beta_T \tilde{\Gamma}_{t-1} + \alpha_T \tilde{z}_{t-1} \tilde{z}_{t-1}^\top.
\] (6.1)

But if we can target the long run correlation \( \tilde{\Gamma} \) to its sample analogue \( \hat{\Gamma} = \frac{1}{T} \sum_{t=1}^{T} \tilde{z}_t \tilde{z}_t^\top \) then we need only to estimate the scalars \( \alpha_T \) and \( \beta_T \) in the numerical MLE procedure.

Recall that \( \tilde{z}_{i,t} = z_{i,t} \sqrt{\tilde{\Gamma}_{ii,t}} \). A circularity problem is apparent because we need \( \tilde{\Gamma}_{ii,t} \) to estimate \( \tilde{\Gamma} \) which in turn is required to compute the time series of \( \tilde{\Gamma}_{ii,t} \). Note however that \( \tilde{\Gamma} \) is a correlation matrix, so that \( \tilde{\Gamma}_{ii} = 1 \), for all \( i \), and note also that only the diagonal elements of \( \tilde{\Gamma}_t \) are needed to compute \( \tilde{z}_{i,t} \). Aielli (2009) therefore proposes to first compute equation (6.1) for the diagonal elements only, that is

\[
\tilde{\Gamma}_{ii,t} = (1 - \alpha_T - \beta_T) + \beta_T \tilde{\Gamma}_{ii,t-1} + \alpha_T \tilde{z}_{i,t-1}^2
\]

for all \( i \) and \( t \). Having computed the \( \tilde{\Gamma}_{ii,t} \), the sample correlation matrix of the \( \tilde{z}_{i,t} \) can be obtained which in turn yields \( \hat{\Gamma} = \frac{1}{T} \sum_{t=1}^{T} \tilde{z}_t \tilde{z}_t^\top \), and the recursion in (6.1) can now be run replacing \( \tilde{\Gamma} \) by \( \hat{\Gamma} \).

Appendix B. The \( t \) Copula

The conventional symmetric \( N \)-dimensional \( t \) distribution has the stochastic representation

\[
X = \sqrt{WZ}
\] (6.2)

where \( W \) is an inverse gamma variable \( W \sim IG \left( \frac{\nu}{2}, \frac{\nu}{2} \right) \), \( Z \) is a normal variable \( Z \sim N \left( 0_N, \Psi \right) \), and where \( Z \) and \( W \) are independent.

The probability density function of the \( t \) copula defined from the \( t \) distribution is given by

\[
c(u; v, \Psi) = \frac{\Gamma \left( \frac{\nu+N}{2} \right)}{\Gamma \left( \frac{\nu}{2} \right) \Gamma \left( \frac{\nu+1}{2} \right)} \left( 1 + \frac{1}{\nu} z^\top \Psi^{-1} z \right)^{-\frac{\nu+N}{2}} \prod_{j=1}^{N} \left( 1 + \frac{z_{j}^2}{\nu} \right)^{-\frac{\nu+1}{2}}
\]
where \( z^* = t_{\lambda,v}^{-1}(u) \) and \( t_v(u) \) is the univariate Student’s \( t \) density function given by

\[
t_v(u) = \int_{-\infty}^{u} \frac{\Gamma \left( \frac{\nu+1}{2} \right)}{\sqrt{\pi} \nu \Gamma \left( \frac{\nu}{2} \right)} \left( 1 + \frac{x^2}{\nu} \right)^{-\frac{\nu+1}{2}} \, dx.
\]

**Appendix C. The Skewed \( t \) Copula**

The skewed \( t \) distribution discussed in Demarta and McNeil (2005) has the more general stochastic representation

\[
X = \sqrt{W}Z + \lambda W
\]

(6.3)

where \( \lambda \) is the asymmetry parameter, \( W \) is again an inverse gamma variable \( W \sim IG \left( \frac{\nu}{2}, \frac{\nu}{2} \right) \), \( Z \) is a normal variable \( Z \sim N(0, \Psi) \), and \( Z \) and \( W \) are again independent. The skewed \( t \) distribution generalizes the \( t \) distribution by adding a second term related to the same inverse gamma random variable which is scaled by an asymmetry parameter \( \lambda \). Note that the conventional symmetric \( t \) distribution is nested when \( \lambda = 0 \).

The probability density function of the skewed \( t \) copula defined from the asymmetric \( t \) distribution is given by

\[
c(u; \lambda, v, \Psi) = \frac{2^{\left(\nu-2\right)N-N-1}}{\Gamma \left( \frac{\nu}{2} \right)^{1-N} |\Psi|^{\frac{1}{2}}} \frac{1}{\left( \nu + z^{*\top} \Psi^{-1} z^* \right)^{\frac{\nu+1}{2}} (1 + \frac{1}{\nu} z^{*\top} \Psi^{-1} z^*)^{\frac{\nu+1}{2}}} \\
\times \prod_{j=1}^{N} \frac{\Gamma \left( \frac{\nu+1}{2} \right) \left( \nu + \left(z_j^*\right)^2 \right)^{\frac{\nu+1}{2}} \left( 1 + \frac{1}{\nu} \left(z_j^*\right)^2 \right)^{\frac{\nu+1}{2}}}{K_\nu \left( \left( \nu + \left(z_j^*\right)^2 \right)^{\frac{\nu+1}{2}} \right) e^{z_j^*\lambda}}
\]

(6.4)

where \( K(\cdot) \) is the modified Bessel function of third kind, and where the fractiles \( z^* = t_{\lambda,v}^{-1}(u) \) are defined from the asymmetric univariate student \( t \) density defined by

\[
t_{\lambda,v}(u) = \int_{-\infty}^{u} \frac{2^{1-\frac{\nu+1}{2}} K_{\nu+1} \left( \left( \nu + x^2 \right)^{\frac{\nu+1}{2}} e^{x\lambda} \right)}{\Gamma \left( \frac{\nu}{2} \right) \sqrt{\pi} \nu \left( \nu + x^2 \right)^{\frac{\nu+1}{2}} \left( 1 + \frac{x^2}{\nu} \right)^{\frac{\nu+1}{2}}} \, dx.
\]

(6.5)

The asymmetric Student \( t \) quantile function, \( t_{\lambda,v}^{-1}(u) \), is not known in closed form but can be well approximated by simulating 100,000 replications of equation 6.3. Note that we constrain the copula to have the same asymmetry parameter, \( \lambda \), across all assets.
The moments of the $W$ variable are given by $m_i = \nu^i / \left( \prod_{j=1}^{i} (\nu - 2j) \right)$, and from the normal mixture structure of the distribution, we can derive the expected value

$$E[X] = E(E[X|W]) = E(W)\lambda = \frac{\nu}{\nu - 2}\lambda$$

and the variance-covariance matrix

$$\text{Cov}(X) = E(\text{Var}(X|W)) + \text{Var}(E[X|W])$$

$$= \frac{\nu}{\nu - 2}\Psi + \frac{2\nu^2\lambda^2}{(\nu - 2)^2(\nu - 4)}.$$ (6.6)

Notice that the covariances are finite if $\nu > 4$. These moments provide the required link between the multivariate asymmetric $t$ distribution and the copula correlation matrix $\Psi$. 
Notes to Figure: We report dynamic equicorrelations (DECOs) for two sample periods. The left-side panels report on the period January 20, 1989 to July 25, 2008. The right-side panels report on the period July 21, 1995 to June 12, 2009. The top panels report on developed markets, the middle panels report on emerging markets, and the bottom panels report on samples consisting of developed and emerging markets.
Figure 2: Comparing DECO and DCC Correlations. Developed Markets. Various Sample Periods

Notes to Figure: We report dynamic equicorrelations (DECOs) and dynamic conditional correlations (DCCs) for sixteen developed markets for three sample periods. The top panels report on the period January 26, 1973 to June 12, 2009. The middle panels report on the period January 20, 1989 to July 25, 2008. The bottom panels report on the period July 21, 1995 to June 12, 2009.
Notes to Figure: We report dynamic conditional correlations for sixteen developed markets for the period January 20, 1989 to July 21, 2008. For each country, at each point in time we report three averages of conditional correlations with other countries: the average of correlations with the fifteen other developed markets (black line), with the thirteen emerging markets (dark grey line), and with the fifteen developed and thirteen emerging markets (light grey line).
Figure 3.B: Correlations for each Emerging Market

Notes to Figure: We report dynamic conditional correlations for thirteen emerging markets for the period January 20, 1989 to July 25, 2008. For each country, at each point in time we report three averages of conditional correlations with other countries: the average of correlations with sixteen developed markets (black line), with the twelve other emerging markets (dark grey line), and with the sixteen developed and twelve emerging markets (light grey line).
Figure 3.C: Regional Correlation Patterns

Notes to Figure: We use the DCC model to plot the average correlation within and across four regions. The European Union (EU) includes Austria, Belgium, Denmark, France, Germany, Ireland, Italy, Netherlands, and the UK. Developed Non-EU includes Australia, Canada, Hong Kong, Japan, Singapore, Switzerland, and the US. Latin America includes Argentina, Brazil, Chile, Colombia, and Mexico. Emerging Eurasia includes India, Jordan, Korea, Malaysia, Philippines, Taiwan, Thailand, and Turkey.
Figure 4: Correlation Range (90th and 10th Percentile). Developed, Emerging and All Markets

Notes to Figure: The shaded areas show the correlation range between the 90th and 10th percentiles for DCCs. The top panels report on sixteen developed markets for the period January 26, 1973 to June 12, 2009. The middle panels report on thirteen emerging markets for the period January 20, 1989 to July 25, 2008. The bottom panels report on sixteen developed and thirteen emerging markets for the period January 20, 1989 to July 25, 2008.
Figure 5: Conditional Diversification Benefits (CDB) using the DCC Model.
Developed, Emerging and All Markets

Notes to Figure: Each week for each set of countries, we use the dynamic conditional correlation (DCC) model to compute the conditional diversification benefits (CDB) as defined in (2.10). The dark line is the CDB computed on the minimum variance portfolio, while the gray line is the CDB measure assuming constant variances and computed on the portfolio maximizing (2.11).
Figure 6: Dynamic Average Bivariate Tail Dependence in skewed t-Copula.
Constant Degree of Freedom

Notes to Figure: We report estimated average bivariate tail dependence for the DCC (left panels) and DECO (right panels) constrained skewed $t$-copula with constant degree of freedom. The black line is the left tail dependence. The gray line is the tail dependence for the right tail. The top panels report on sixteen developed markets, the middle panels report on thirteen emerging markets, and the bottom panels report on sixteen developed and thirteen emerging markets for the period January 20, 1989 to July 25, 2008.
Figure 7: DECO and Spline DECO Correlations for Developed, Emerging, and All Markets

Notes to Figure: We report the DECO and spline DECO correlations for the period January 20, 1989 to July 25, 2008. The left panels correspond to the DECO model with a fixed long run average, and the right panels are equicorrelations from the Spline DECO. The top panel reports on developed markets, the second panel reports on emerging markets, the third on all markets. In the right panels, the black line shows the total correlation while the gray line shows the long-run correlation mean.
Notes to Figure: We report rolling correlations for two sample periods. The left-side panels report on the period January 20, 1989 to July 25, 2008. The right-side panels report on the period July 21, 1995 to June 12, 2009. The top panels report on developed markets, the middle panels report on emerging markets, and the bottom panels report on samples consisting of developed and emerging markets. We use 6-month (grey lines) and 2-year (black lines) windows to estimate rolling correlations for each pair of markets which are then averaged across pairs to produce the plot.
### Table 1: Descriptive Statistics for Weekly Returns on 16 DM and 13 EM (IFCG)
January 1989 to July 2008

<table>
<thead>
<tr>
<th>Developed Markets</th>
<th>Annual Mean (%)</th>
<th>Annual Standard Deviation (%)</th>
<th>Skewness</th>
<th>Excess Kurtosis</th>
<th>1st Order Autocorrelation</th>
<th>LB(20) P-value on Returns</th>
<th>LB(20) P-value on Absolute Returns</th>
</tr>
</thead>
<tbody>
<tr>
<td>Australia</td>
<td>13.21</td>
<td>17.13</td>
<td>-0.301</td>
<td>1.94</td>
<td>-0.010</td>
<td>0.2044</td>
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<tr>
<td>Austria</td>
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<td>19.63</td>
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<td>3.69</td>
<td>0.058</td>
<td>0.1364</td>
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<td>Belgium</td>
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<td>2.00</td>
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</tr>
<tr>
<td>Canada</td>
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<td>0.1611</td>
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<tr>
<td>Denmark</td>
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<td>17.83</td>
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<td>0.2535</td>
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<tr>
<td>France</td>
<td>12.75</td>
<td>17.54</td>
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<td>1.04</td>
<td>0.019</td>
<td>0.0632</td>
<td>0.0000</td>
</tr>
<tr>
<td>Germany</td>
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<td>18.66</td>
<td>-0.231</td>
<td>1.65</td>
<td>0.018</td>
<td>0.7596</td>
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<td>Hong Kong</td>
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<td>3.11</td>
<td>0.030</td>
<td>0.0046</td>
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<tr>
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<tr>
<td>Italy</td>
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<td>20.99</td>
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<td>3.32</td>
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<td>0.1494</td>
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<tr>
<td>Japan</td>
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<tr>
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<td>0.3920</td>
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<tr>
<td>Singapore</td>
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<td>20.66</td>
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<td>5.15</td>
<td>-0.009</td>
<td>0.0010</td>
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<tr>
<td>Switzerland</td>
<td>13.70</td>
<td>16.42</td>
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<td>2.05</td>
<td>-0.012</td>
<td>0.5579</td>
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</tr>
<tr>
<td>United Kingdom</td>
<td>11.37</td>
<td>15.54</td>
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<td>1.80</td>
<td>-0.027</td>
<td>0.6799</td>
<td>0.0019</td>
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<tr>
<td>United States</td>
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<td>15.15</td>
<td>-0.434</td>
<td>3.46</td>
<td>-0.102</td>
<td>0.0005</td>
<td>0.0000</td>
</tr>
<tr>
<td><strong>Average</strong></td>
<td><strong>12.06</strong></td>
<td><strong>18.41</strong></td>
<td><strong>-0.170</strong></td>
<td><strong>2.50</strong></td>
<td><strong>-0.005</strong></td>
<td><strong>0.2813</strong></td>
<td><strong>0.0001</strong></td>
</tr>
</tbody>
</table>

### Emerging Markets

<table>
<thead>
<tr>
<th>Emerging Markets</th>
<th>Annual Mean (%)</th>
<th>Annual Standard Deviation (%)</th>
<th>Skewness</th>
<th>Excess Kurtosis</th>
<th>1st Order Autocorrelation</th>
<th>LB(20) P-value on Returns</th>
<th>LB(20) P-value on Absolute Returns</th>
</tr>
</thead>
<tbody>
<tr>
<td>Argentina</td>
<td>29.44</td>
<td>51.18</td>
<td>0.804</td>
<td>12.22</td>
<td>-0.009</td>
<td>0.0001</td>
<td>0.0000</td>
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<tr>
<td>Brazil</td>
<td>29.85</td>
<td>46.23</td>
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<td>2.22</td>
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<td>0.3060</td>
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<tr>
<td>Chile</td>
<td>19.43</td>
<td>21.18</td>
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<td>1.30</td>
<td>0.167</td>
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<td>0.0000</td>
</tr>
<tr>
<td>Colombia</td>
<td>22.66</td>
<td>26.51</td>
<td>0.339</td>
<td>6.29</td>
<td>0.132</td>
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<td>0.0000</td>
</tr>
<tr>
<td>India</td>
<td>15.24</td>
<td>27.89</td>
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<td>2.05</td>
<td>0.078</td>
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<tr>
<td>Jordan</td>
<td>15.86</td>
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<td>5.42</td>
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<tr>
<td>Korea</td>
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<td>36.43</td>
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<td>8.54</td>
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<td>0.0001</td>
<td>0.0000</td>
</tr>
<tr>
<td>Malaysia</td>
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<td>4.97</td>
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<td>0.0002</td>
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<tr>
<td>Taiwan</td>
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<td>32.82</td>
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<td>3.96</td>
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<tr>
<td>Thailand</td>
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<td>Turkey</td>
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<td>5.27</td>
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<tr>
<td><strong>Average</strong></td>
<td><strong>17.68</strong></td>
<td><strong>33.63</strong></td>
<td><strong>0.191</strong></td>
<td><strong>6.46</strong></td>
<td><strong>0.047</strong></td>
<td><strong>0.0445</strong></td>
<td><strong>0.0000</strong></td>
</tr>
</tbody>
</table>

Notes to Table: We report the first four sample moments and the first order autocorrelation of the 16 DM and 13 EM (IFCG) returns. We also report the p-value from a Ljung-Box test that the first 20 autocorrelations are zero for returns and absolute returns. The sample period is from January 20, 1989 to July 25, 2008.
### Table 2: Parameter Estimates from NGARCH(1,1) on 16 DM and 13 EM (IFCG)

January 1989 to July 2008

<table>
<thead>
<tr>
<th>Developed Markets</th>
<th>α</th>
<th>β</th>
<th>θ</th>
<th>Variance Persistence</th>
<th>LB(20) P- Value on Residuals</th>
<th>RES(20) P- Value on Absolute Residuals</th>
<th>Residual Skewness</th>
<th>Residual Excess Kurtosis</th>
</tr>
</thead>
<tbody>
<tr>
<td>Australia</td>
<td>0.055</td>
<td>0.804</td>
<td>0.785</td>
<td>0.893</td>
<td>0.633</td>
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<tr>
<td>Austria</td>
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<td>0.898</td>
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<td>0.978</td>
<td>0.442</td>
<td>0.321</td>
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</tr>
<tr>
<td>Belgium</td>
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<td>0.737</td>
<td>0.804</td>
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<tr>
<td>Canada</td>
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<td>0.847</td>
<td>0.323</td>
<td>0.958</td>
<td>0.638</td>
<td>0.825</td>
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</tr>
<tr>
<td>Denmark</td>
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<td>0.941</td>
<td>0.027</td>
<td>0.990</td>
<td>0.342</td>
<td>0.477</td>
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<tr>
<td>France</td>
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<td>0.697</td>
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<td>0.866</td>
<td>0.124</td>
<td>0.374</td>
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<td>0.28</td>
</tr>
<tr>
<td>Germany</td>
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<td>0.557</td>
<td>0.903</td>
<td>0.814</td>
<td>0.101</td>
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</tr>
<tr>
<td>Hong Kong</td>
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<td>0.810</td>
<td>0.530</td>
<td>0.955</td>
<td>0.231</td>
<td>0.537</td>
<td>-0.320</td>
<td>1.20</td>
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<tr>
<td>Ireland</td>
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<td>Italy</td>
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### Emerging Markets

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<th>θ</th>
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<th>LB(20) P- Value on Residuals</th>
<th>RES(20) P- Value on Absolute Residuals</th>
<th>Residual Skewness</th>
<th>Residual Excess Kurtosis</th>
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<td>0.633</td>
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Notes to Table: We report parameter estimates and residual diagnostics for the NGARCH(1,1) models. The sample period for 16 DM and 13 EM (IFCG) weekly returns is from January 20, 1989 to July 25, 2008. The conditional mean is modeled by an AR(2) model. The coefficients from the AR models are not shown. The constant term in the GARCH model is fixed by variance targeting.

<table>
<thead>
<tr>
<th>Markets</th>
<th>( \alpha_\Gamma )</th>
<th>( \beta_\Gamma )</th>
<th>Persistence</th>
<th>Composite Likelihood</th>
<th>( \alpha_\Gamma )</th>
<th>( \beta_\Gamma )</th>
<th>Persistence</th>
<th>Composite Likelihood</th>
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Notes to Table: We report parameter estimates for the DCC and DECO models for the 13 emerging markets (IFCG), 17 emerging markets (IFCI), 16 developed markets, and all markets. The composite likelihood is the average of the quasi-likelihoods (correlation log likelihood + all marginal volatility log likelihood) of all unique pairs of assets. We also report the special case of no dynamics.

<table>
<thead>
<tr>
<th></th>
<th>A: DCC t-Copula</th>
<th>B: DCC Skewed t-Copula</th>
<th>Composite Likelihood</th>
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<td>ν</td>
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<table>
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<th>D: DECO Skewed t-Copula</th>
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<td>Persistence</td>
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<td>No Dynamics</td>
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<table>
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<th>E: DECO t-Copula with Dynamic Degree of Freedom</th>
<th>F: DECO Skewed t-Copula with Dynamic Degree of Freedom</th>
<th>Composite Likelihood</th>
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Notes to Table: We report parameter estimates for the DECO and DCC t-copula and constrained skewed t-copula models for the 13 emerging markets (IFCG), 16 developed markets, and all markets. The bottom panel presents the results with dynamic degree of freedom. The composite likelihood is the average of the quasi-likelihoods (copula log likelihood + all marginal QML log likelihoods) of all pairs of assets. We also report the special case of each model with no dynamics.
<table>
<thead>
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<th>Time Trend</th>
<th>MCR</th>
<th>EMI</th>
<th>Vol DMs</th>
<th>Vol EMs</th>
<th>Vol All</th>
<th>Vol(i)</th>
<th>R²</th>
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Panel A: Regressand: Average Monthly Emerging Market DCC Correlation with all other Emerging Markets

<table>
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<th>Time Trend</th>
<th>MCR</th>
<th>EMI</th>
<th>Vol DMs</th>
<th>Vol EMs</th>
<th>Vol All</th>
<th>Vol(i)</th>
<th>R²</th>
</tr>
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Panel B: Regressand: Average Monthly Emerging Market DCC Correlation with all Developed Markets

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<th>Vol DMs</th>
<th>Vol EMs</th>
<th>Vol All</th>
<th>Vol(i)</th>
<th>R²</th>
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</thead>
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Panel C: Regressand: Average Monthly Emerging Market DCC Correlation with all other Markets

Note to Table: We estimate panel regressions for the 17 emerging markets in the IFCI index from August 1995 to December 2006. Country fixed effects are included in each specification, and White standard errors adjusted for within cluster correlations are provided in parentheses. "MCR" denotes the ratio of market capitalizations of the S&P/IFC investable index to the S&P/IFC global index. "EMI" denotes the integration measure implied by the Errunza and Losq (1985) model. We also include a time trend, and different measures of volatilities as controls. Each measure of weekly correlation is averaged for the month. Vol DMs, Vol EMs, and Vol All are the equally-weighted averages of log monthly volatilities across all DMs, all EMs and all markets respectively. Vol(i) is the market specific log monthly volatility. * indicates significance at the 5% level, and ** indicates significance at the 1% level.
Emerging Markets, Developed Markets, and All Markets

<table>
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<tr>
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<th>$w_0$</th>
<th>$w_1$</th>
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<td>0</td>
<td>0</td>
<td>0.3027</td>
<td>1.30E-04</td>
<td>8.39E-07</td>
<td>4345.69</td>
</tr>
</tbody>
</table>

Notes to Table: We report parameter estimates for the spline DECO models for the 13 emerging markets (IFCG), 16 developed markets, and all 29 markets. The composite likelihood is the average of the quasi-likelihoods (correlation log likelihood + all marginal volatility log likelihood) of all unique pairs of assets. We also report the special case of no stochastics ($\alpha_\Gamma=\beta_\Gamma=0$) where the spline captures all the dynamics in the correlations.